Design of an ultra-low power device for aircraft structural health monitoring

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Abstract—One of the popular structural health monitoring (SHM) applications of both automotive and aeronautic fields is devoted to the non-destructive localization of impacts in plate-like structures. The aim of this paper is to develop a miniaturized, self-contained and low power device for automated impact detection that can be used in a distributed fashion without central coordination. The proposed device uses an array of four piezoelectric transducers, bonded to the plate, capable to detect the guided waves generated by an impact, to a STM32F4 board equipped with an ARM Cortex-M4 microcontroller and a IEEE802.15.4 wireless transceiver. The waves processing and the localization algorithm are implemented on-board and optimized for speed and power consumption. In particular, the localization of the impact point is obtained by cross-correlating the signals related to the same event acquired by the different sensors in the warped frequency domain. Finally the performance of the whole system is analysed in terms of localization accuracy and power consumption, showing the effectiveness of the proposed implementation.

I. INTRODUCTION

Damages to aircraft and high-speed vehicles caused by the impact of debris and flying objects is a critical concern for automotive and aeronautic systems. Such damages, in fact, if not detected and repaired at an early stage might grow leading to the failure of the systems. In this context, Structural health monitoring (SHM) technologies, by embedding smart sensors into the structures and responding/adapting to changes in condition, can allow for an automatic detection of defects due to impacts. Among the number of SHM approaches, the one based on guided waves (GW) is considered as the most promising and versatile. In fact, an impact at high speed produces detectable acoustic and ultrasonic guided waves on the structural component. These waves can be used to compute the location of the impact and eventually to assess the damage. In general, GW based technologies for SHM exploit a network of piezoelectric transducers positioned on the structure to inspect. The minimization of the array elements is fundamental to reduce not only the hardware complexity associated with transducer wiring and multiplexing circuitry but also the intensive signal processing of the large amounts of recorded data. For this reason, there is growing interest in minimizing the number of sensors by optimizing their positioning, as well as by increasing the resolution of impact localization procedures [1]. Another current trend in the SHM field is to create wireless sensor networks with low power consumption or even energetically autonomous [2], [3]. One promising solution would be a SHM system that could be embedded into the structure, inspect the structural hot spots and download data or diagnostic results wirelessly to a remote station [4], [5], [6]. A lot of literature has been produced on the use of sensor-array-based methods for high-speed acquisition and data processing. However, generally such approaches use a large number of individual sensors that usually are bulky, heavy and require wiring back to a central location. Moreover when large-scale deployment are implied, the power consumption of the system is hardly sustainable by the ordinary generation system present on board. In contrast to these traditional transducers, wireless sensors technology integrating small sensors and wireless communication are becoming vital in SHM, guaranteeing at the same time: (1) less wiring among sensors and between sensors and the central unit; (2) lower weight; (3) reduced power consumption and (4) real-time monitoring even in harsh environmental conditions.

In this paper we propose a new PZT-based wireless embedded ultrasonic structural monitoring system for impact localization with advantages over traditional systems of compactness, light weight, low-power consumption and high efficiency and precision. The passive approach based on ultrasonic Lamb waves and conventional piezoelectric transducers (PZT discs) is capable of achieving high localization performance using a dispersion compensation algorithm with low computational cost. The structure of the SHM system is illustrated in Fig. 1. In the new SHM system, the signal conditioning, amplification and A/D converting circuits are replaced by a simple comparator circuit, in which the response signal from a piezoelectric transducer PZT sensor is directly changed into a digital queue by comparing it with a preset trigger value.

![Fig. 1. Structure of the embedded SHM system for impact detection](image)

The device samples the signals in passive mode using 4 different piezoelectric transducers and the signals are elaborated on a Cortex-M4 based microcontroller. By cross-correlating
the dispersion-compensated signals, the impact point can be determined via hyperbolic positioning. Thus, when an impact occurs, only the data of its position is recorded and sent to the central system through wireless transmission. The structure of this paper is as follows: in Section II the proposed compensation procedure based on the Warped Frequency Transform (WFT) is presented. The design and realization of the new PZT-based wireless digital impact monitoring system is described in detail in Section III. Section IV shows the feasibility and stability of the embedded ultrasonic structural monitoring system and an experimental validation is presented.

II. DISPERSION COMPENSATION USING THE WARPED FREQUENCY TRANSFORM

A. The warping frequency transform (WFT)

Given a dispersive guided wave signal \( s(t) \) whose frequency representation is \( S(f) = F \{ s(t) \} \), being \( F \) the Fourier Transform operator, the Frequency Warping operator \( W_w \) reshapes the periodic frequency axis by means of a proper function \( w(f) \), called from now warping map, such as:

\[
  s_w(t) = W_w \{ s(t) \} \quad \text{and} \quad F \{ s_w(t) \} \equiv \sqrt{w(f)} \cdot S(w(f))
\]

where \( s_w(t) \) is the warped signal, and \( w(f) \) represents the first derivative of \( w(f) \). The Frequency Warping operator can be expressed as the composition of the Non-Uniform Fourier Transform (NUFFT) \( F_w \) and the classical Inverse Fourier Transform \( F^\dagger \):

\[
  W_w = F^\dagger F_w
\]

It has been shown in [7], [8] that in order to compensate the signal with respect to a particular guided mode, \( w(f) \) can be defined through its functional inverse, as:

\[
  K \frac{dw^{-1}(f)}{df} = \frac{1}{c_g(f)}
\]

where \( \frac{1}{c_g(f)} \) is the nominal dispersive slowness relation of the wave to consider, being \( c_g(f) \) its group velocity curve and \( K \) a normalization parameter selected so that \( w^{-1}(0.5) = w(0.5) = 0.5 \).

A sample warping map is depicted in Fig. 2 along with its functional inverse \( w^{-1}(f) \). It was computed according to Eq. (2) by considering the group velocity curve of the Lamb \( A_0 \) mode represented in Fig. 3. The curves in Fig.3 were obtained by using the Semi-Analytical Finite Element (SAFE) formulation proposed in [9] considering a 0.003 m thick aluminum plate with Young modulus \( E = 69 \) GPa, Poisson’s coefficient \( \nu = 0.33 \) and material density \( \rho = 2700 \) kg \( \cdot \) m\(^{-3} \).

The NUFFT is based on an oversampled Discrete Fourier Transform (DFT) followed by an interpolation method optimal in the min-max sense of minimizing the worst-case approximation error over all signals of unit norm [10]. To compute the DFT at a collection of (non uniformly spaced) frequency locations \( \omega_m \) which represent the warping map \( w(f) \), first a convenient \( K \geq N \) must be assumed so that the \( K \)-point FFT of \( S(\omega_k) = F \{ s_n \} = \sum_{n=0}^{N-1} s_n e^{-j \frac{2\pi}{N} k n} \quad k = 1, \ldots, K \) where \( \frac{2\pi}{N} \) is the fundamental frequency of the \( K \)-point DFT. The second step of most NUFFT methods is to approximate each \( S(\omega_m) \) by interpolating \( S(\omega) \) using some of the neighbors of \( \omega_m \) in the DFT frequency set. Linear interpolators have the following general form:

\[
  \hat{S}(\omega_m) = \sum_{k=0}^{K-1} u_k(\omega_m) S(\omega_k) \quad m = 1, \ldots, M
\]

where the \( u_k(\omega_m) \) denote the interpolation coefficients selected through a min-max criterion. For each desired frequency location \( \omega_m \) the coefficient vector the worst-case approximation error between \( S(\omega_m) \) and \( S(\omega_m) \) is determined. As demonstrated in [10], the interpolator coefficients \( u_k(\omega_m) \) can be obtained by an analytic formula derived from the following optimization criterion:

\[
  \min_{u(\omega_m) \in C} \max_{\omega \in \mathbb{R}} |S(\omega_m) - \hat{S}(\omega)|
\]

B. Warping a wave detected passively

In passive monitoring techniques the time instant in which an acoustic emission starts is unknown. Let us consider the effect of warping when an actuated wave is excited at a generic instant \( t_{d1} \). The Fourier Transform of the actuated wave is given by: \( S_n(f, 0) = S_0(f, 0) \cdot e^{-j2\pi t_{d1} f} \) being \( S_0(f, 0) \) the Fourier Transform of the excited wave (incipient pulse centered in \( t = 0 \)). An undamped guided wave at a traveled distance \( D \) from the source point, \( s(t, D) \), can be modeled in the frequency domain as a dispersive system whose response is:

\[
  S(f, D) = S_0(f, 0) \cdot e^{-j2\pi t_{d1} f} \cdot e^{-j2\pi f \tau(f, D) df}
\]

being \( \tau(f, D) \) the group delay of the wave component of frequency \( f \) which can be assumed equal to:

\[
  \tau(f, D) = \frac{D}{c_g(f)} = D \cdot K \cdot \frac{dw^{-1}(f)}{df}
\]

In force of Eq. (3), (4) can be rewritten as:

\[
  S(f, D) = S_0(f, 0) \cdot e^{-j2\pi t_{d1} f} \cdot e^{-j2\pi w^{-1}(f)KD}
\]

where the distortion results from the nonlinear phase term. Considering now that the generated dispersive wave \( s(t, D) \) is acquired by two different sensors (1 and 2) after having travelled two different distances of propagation, \( D_1 \) and \( D_2 \). The Warped Fourier Transforms of the recorded signals \( s(t, D_1) \) and \( s(t, D_2) \) are given by:

\[
  \mathbf{FW}_w \{ s(t, D_1) \} = \sqrt{w(f)} \cdot S_0(w(f), 0) \cdot e^{-j2\pi w(f) t_{d1}} \cdot e^{-j2\pi fKD_1},
\]
\[
  \mathbf{FW}_w \{ s(t, D_2) \} = \sqrt{w(f)} \cdot S_0(w(f), 0) \cdot e^{-j2\pi w(f) t_{d1}} \cdot e^{-j2\pi fKD_2}
\]
where the right hand terms can be distinguished only for the underlined distance-dependent linear phase shifts, which causes simple translations of the warped signals on the warped time axis. This property can be fruitfully exploited by using signal correlation techniques and Eq. (1), since in the frequency domain the cross-correlation of two warped signals $s_w = s_{w1} \times s_{w2}$ is:

$$F \{s_w\} = Fw \{s(t, D_1)\} \cdot (Fw)^* \{s(t, D_k)\}$$

$$= Fw \{s(t, D_2)\} \cdot (Fw)^* \{s(t, D_k)\}$$

$$= \hat{w}(f) \cdot |S_0(w(f), 0)|^2 \cdot e^{-j2\pi f K(D_1 - D_k)}$$

Thus, the abscissa value at which the cross-correlation envelope of two signals peaks in the warped domain can be directly related to the difference in distance of propagation by the two dispersive signals. The algorithm graph is shown in Fig. 4.

![Graph of the proposed localization algorithm](image)

**Fig. 4.** Graph of the proposed localization algorithm

### C. Hyperbolic positioning

Given the coordinates of the sensors positions $(x_i, y_i)$ and having estimated the differences in traveled distance $\Delta d_i$ between the waves acquired by the first sensor and the remaining, a hyperbolic positioning method (also called multilateration) can be applied to locate the point source.

$$\Delta d_i = \sqrt{(x_1 - x_p)^2 + (y_1 - y_p)^2} - \sqrt{(x_i - x_p)^2 + (y_i - y_p)^2}$$

The intersection of the different hyperbolas, obtained by solving the system of $M - 1$ equations (where $M$ is the number of sensors) with the Levenberg-Marquardt algorithm [11], is taken to be the impact position.

### III. HARDWARE DESIGN

The system is composed by 4 different elements: (A) piezoelectric sensors, (B) acquisition chain, (C) processing electronic unit and (D) wireless transmission module.

#### (A) Piezoelectric sensors: when an impact occurs on an elastic structure, a stress wave is created and it propagates across the structure, radially from the point of impact. The proposed system exploits at least 4 conventional piezoelectric transducers arranged in a geometrical fashion.

#### (B) Acquisition chain: PZT transducers are connected directly with the ADC ports of the STM32F4 board and each ADC channel is configured in dual mode with 250 kHz maximum sampling frequency since generally the spectral components of the Lamb waves lower rapidly above 60-100 kHz. The acquired values are stored in a DMA circular buffer; when the maximum value of the buffer exceeds the threshold value the trigger is sent and the Micro Controller Unit (MCU) performs the localization algorithm. The acquisition settings are shown in Table I:

<table>
<thead>
<tr>
<th>Inputs</th>
<th>4 sensors</th>
<th>Sampling frequency $f_s$</th>
<th>250 kHz</th>
</tr>
</thead>
<tbody>
<tr>
<td>Input Range</td>
<td>$\pm 2$</td>
<td>Samples</td>
<td>2048</td>
</tr>
</tbody>
</table>

#### (C) Processing electronic unit: the center of the system is the processing core which contains function modules for data collection, processing and communication control. A Cortex-M4 based board is selected as main chip in the processing core. The MCU is specifically a STM32F4 evaluation board featuring a STM32F407VGT6 microcontroller with 1 MB Flash and 192 KB RAM. The strength point of the core is the CPU with FPU, adaptive real-time accelerator allowing 0-wait state execution from Flash memory and frequency up to 168 MHz. The computational cost of the proposed localization algorithm is shown in Table II.

<table>
<thead>
<tr>
<th>Algorithm computational cost</th>
<th>Non Uniform FFT</th>
<th>MIN-MAX</th>
<th>Cross-Correlation</th>
<th>Inverse FFT</th>
</tr>
</thead>
<tbody>
<tr>
<td>$N = J \times M = 2^{12}$ points: complexity $O(N \log N)$</td>
<td>$J \times M = 2^{12}$; complexity $O(JM)$</td>
<td>$M \log_2(M)$</td>
<td>$2^{12} \times 12 \approx 49$ KByte</td>
<td>$2^{12}$ points complexity $O(M \log M)$</td>
</tr>
</tbody>
</table>

#### (D) Wireless transmission module: when the device is used to monitor the structural health of large structures, each node in the network monitors a specific portion of the structure surface, eventually reporting to a central location in case of detected damage. The wireless communication technology allows long distance data transmission without wiring, simplifying the difficulties in multi-device network monitoring. To be compliant with the power requirements the device presents a RF wireless module ZigBee/IEEE802.15.4 compliant, connected to the main board using an Serial Peripheral Interface (SPI).

### IV. EXPERIMENTAL VERIFICATION

We exploited the proposed SHM system to locate impacts in an aluminum 1050A square plate 1 m $\times$ 1 m and 3 mm thick. Four PZT discs (PIC181, diameter 10 mm, thickness 1 mm) were placed asymmetrically at the corners of a square as depicted in the experimental setup in Fig. 5.

![Experimental setup](image)
acquisitions triggered when the signal received from one of the 
PZT discs reached a threshold level of 50 mV. In order 
to analyse the dependency of the power consumption and 
the localization performances with the sampling frequency, 
experiments were carried changing the frequency in the range 
[150 – 250] kHz. Results in Table III show how lowering 
the sampling frequency, the current consumption decreases but not 
in a linear manner; furthermore the MCU elaboration step is 
very sensible to the sampling frequency since the algorithm 
complexity is proportional to the sample buffer length which 
is reduced if the sampling frequency is lower.

<table>
<thead>
<tr>
<th>TABLE III. MEAN CURRENT CONSUMPTION</th>
</tr>
</thead>
<tbody>
<tr>
<td>f_s = 250 kHz</td>
</tr>
<tr>
<td>32 mA</td>
</tr>
<tr>
<td>f_s = 200 kHz</td>
</tr>
<tr>
<td>f_s = 150 kHz</td>
</tr>
</tbody>
</table>

Fig. 6 shows the current consumption values measured for 
different sampling frequencies. Since the ADC sampling state 
is performed always in time the current reduction achieved 
with low frequency is noticeable. However, such reduction 
must be analysed with respect to the resolution achieved in 
the impact localization.

As it can be seen from Fig. 7, lowering the sampling frequency 
the positioning error rises; in contexts such as wing monitoring, 
the high localization resolution is an important constrain 
because facilitates the decision to be taken in critical phases such 
as aircraft takeoff and optimizes the number of sensors 
to be used to monitor large areas.

In Fig. 7 is reported the mean error of the difference distance of 
arrival measured on a set of K = 10 of experimental impacts 
on the aluminum plate. The error is calculated as follow:

\[ e = \frac{1}{3 \times K} \sum_{k=1}^{K} \sum_{i=1}^{3} (\Delta d_{1i} - \Delta d_{2i}) \quad k = 1, \ldots, 10; \]

A good parameter able to take into account both the 
current consumption and the spatial resolution is \( I_{\Delta}(mA) \) \( e(\text{mm}) \). Fig.
8 shows that \( I_{\Delta}(mA) \) is not constant, denoting that the impact 
localization error and the current consumption tends to be 
quadratic. Fig. 9 shows the dependency of \( I_{\Delta}(mA) \) \( e(\text{mm}) \) with the 
sampling frequency.

V. CONCLUSIONS

In this work an efficient wireless embedded structural 
monitoring system for impact localization based on Lamb 
waves is proposed. The method applies a dispersion compen-
sation procedure on the signals acquired by passive sensors, 
thus overcoming the difficulties associated with arrival time 
detection based on classical thresholding procedures. The 
processing framework and the algorithm are implemented on 
a STM32F4 discovery board with advantages of compactness, 
low-power consumption, high efficiency and precision. The 
system was validated experimentally to locate impacts in a 
aluinum plate with four sparse PZT sensors. Results shows the 
effectiveness of the proposed implementation with high 
localization accuracy and low current consumption.

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