An Area Optimized Reconfigurable Encryptor for AES-Rijndael

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Abstract

This paper presents a reconfigurable architecture of the Advanced Encryption Standard (AES-Rijndael) cryptosystem. The suggested reconfigurable architecture is capable of handling all possible combinations of standard bit lengths (128,192,256) of data and key. The fully rolled inner-pipelined architecture ensures lesser hardware complexity. The work develops a FSMD model based controller which is ideal for such iterative implementation of AES. S-boxes here have been implemented using combinatorial logic over composite field arithmetic which completely eliminates the need of any internal memory. The design has been implemented on Xilinx Vertex XCV1000 and 0.18µ CMOS technology. The performance of the architecture has been compared with existing results in the literature and has been found to be the most compact implementations of the AES algorithm.

1 Introduction

Rijndael block cipher algorithm [2] has been chosen by NIST as the new Advanced Encryption Standard (AES). It is a symmetric block cipher that can process 128, 192 and 256 bits message blocks and 128, 192, and 256 bits key lengths. Hardware implementation of AES is attractive since software implementation [1] is relatively slow. It is desirable to have reconfigurable AES architectures that can work under various combinations of block and key lengths.

Many FPGA [4, 9, 11] and ASIC [3, 5, 13, 14, 16] implementations for Rijndael have been reported to date. Without exploiting composite field arithmetic most of them have used look up tables to implement the non-linear S-box operations in their architecture, resulting in larger area requirements. Moreover, these implementations can only process blocks of 128 bits and keys of the same length. The effective application of composite field $GF((2^4)^2)$ arithmetic in S-box operation was proposed by Rudra et al. [5]. Among those who tried to produce a really compact implementation using composite field arithmetic, the works of Satoh et al. [6] and Wolkerstorfer et al. [7] can only process 128 bits block and key lengths. The reconfigurable AES Rijndael architecture proposed in this paper can process all nine combinations of key and data lengths. The effective use of composite field $GF((2^4)^2)$ helps to reduce the hardware complexity of the architecture.

The remainder of this paper is organized as follows. In Section 2, AES algorithm is briefly described. In Section 3 an overview of the architecture is presented. Section 4 discusses the encryption unit. Section 5 explains how round keys are generated. Section 6 explores the FSMD model to generate the control signals. Section 7 analyzes the results, followed by concluding remarks in section 8.

2 AES-Rijndael Algorithm

AES-Rijndael [2] can support variable block and key lengths of 128, 192 or 256-bits. The round transformation consists of four different transformations: ByteSub, ShiftRow, MixColumn and AddRoundKey. They are performed in this order with the exception of the final round which is slightly different. All transformations are based on byte-oriented operations. AddRoundKey consists of bitwise XOR operations. The transformations operate on the intermediate result, which is called the State. The ByteSub transformation is a non-linear byte substitution, also called S-box. The S-box is invertible and consists of the following two operations:

- Inversion in the $GF(2^8)$ field, modulo the irreducible polynomial $m(x) = x^8 + x^4 + x^3 + x + 1$.
- Affine transformation defined as: $Y = AX^{-1} + B$, where $A$ is an $8 \times 8$ fixed matrix and $B$ is an $8 \times 1$ vector-matrix.

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### 3 Design Overview

#### 3.1 Key Scheduler

The key scheduler generates the round keys for each round of encryption. It takes the initial key and rounds it to generate the necessary round keys. The key scheduler is implemented using a linear feedback shift register (LFSR) and a multiplexor (MUX) to select the appropriate sub-keys for each round.

#### 3.2 Data Scheduler

The data scheduler organizes the input data into blocks and ensures that the correct data is available for each encryption stage. It is responsible for shifting the data block to the correct position for each round of encryption.

#### 3.3 Cipher Text Processor

The cipher text processor is responsible for processing the cipher text output from the encryption unit. It includes operations such as AES decryption and Key Schedule.

### 4 Encryption Unit

The encryption unit is fully modeled to support all standard modes of encryption operation including CBC, OFB etc.

#### 4.1 S-box Design on Composite Fields

The major computation inside S-box is to find out the multiplicative inverse of an element in the finite field $GF(2^8)$. It is the most costly operation in terms of hardware and power [16]. For reducing cost associated with this operation, several authors have designed AES S-boxes based on composite field techniques [6, 7, 10]. The techniques use three-stage strategy (Figure 3):

- Map the element $X \in GF(2^8)$ to a composite field $F \in GF(2^4)^2$ using an isomorphic function $\delta$ [6].
- Compute the multiplicative inverse over the field $F \in GF(2^4)^2$.
- Finally map the computation result back to the original field using the inverse function $\delta^{-1}$.

The primary drawback of these technique is that for processing 128-bit data in ByteSub operations, 32 isomorphic elements are necessary.

### Table 1. Shift offsets for different blocks

<table>
<thead>
<tr>
<th>Block Size</th>
<th>Offset 1</th>
<th>Offset 2</th>
<th>Offset 3</th>
<th>Offset 4</th>
</tr>
</thead>
<tbody>
<tr>
<td>128</td>
<td>1-Byte</td>
<td>2-Byte</td>
<td>3-Byte</td>
<td>4-Byte</td>
</tr>
<tr>
<td>192</td>
<td>1-Byte</td>
<td>2-Byte</td>
<td>3-Byte</td>
<td></td>
</tr>
<tr>
<td>256</td>
<td>1-Byte</td>
<td>2-Byte</td>
<td>3-Byte</td>
<td>4-Byte</td>
</tr>
</tbody>
</table>

In ShiftRow, the rows of the State are cyclically shifted over different offsets (Table 1 [2]); row 0 is not shifted.

The MixColumn transformation operates on each column of State individually. Each column of the State matrix is multiplied by a fixed matrix $M$ and it is defined as:

$$ M = \begin{pmatrix} 2 & 3 & 1 & 1 \\ 1 & 2 & 3 & 1 \\ 1 & 1 & 2 & 3 \\ 3 & 1 & 1 & 2 \end{pmatrix} $$

#### Figure 1. Top-Level Architecture

The encryption data path processes 32-byte block in parallel. A complete round transformation executes in two clock cycles. Each transformation is optimized appropriately for maximal performance. The data flow through various parts of the unit are controlled by three control signals, namely DataEnable, AddKeyEnable and LastRound, that are generated by the control unit. Due to its rolling technique the design can support all standard modes of encryption operation including CBC, OFB etc.

#### Figure 2. The Encryption Unit

During encryption, the data are organized conceptually in an 4x8 matrix of bytes. This organization is used for data block sizes of 256 bits. For smaller data block sizes (128 or 192 bits), the leftmost columns of the matrix are unused. The encryption unit is fully rolled which ensures a reduction in hardware. It has been implemented with inner pipelining technique for reduction of the combinational path delay. The encryption data path processes 32-byte block in parallel.
functions (δ and δ⁻¹) are to be used parallely, 16 for mapping \(GF(2^8)\) elements to \(GF((2^4)²)\) elements and 16 for reverse conversion.

On the contrary our design uses only two isomorphic functions δ and δ⁻¹, one in DataScheduler and another in DataConverter (Figure 1). The function δ converts an element \(x\) in \(GF(2^8)\) to an element in \(GF((2^4)²)\) [8]. The function δ is defined as \(δ(x) = T.x\), where \(T\) is a transformation matrix and defined as:

\[
T = \begin{pmatrix}
1 & 0 & 1 & 1 & 1 & 0 & 1 & 1 \\
0 & 1 & 0 & 1 & 0 & 0 & 0 & 0 \\
0 & 1 & 0 & 0 & 1 & 0 & 1 & 0 \\
0 & 1 & 1 & 0 & 0 & 0 & 1 & 1 \\
0 & 0 & 0 & 0 & 1 & 1 & 0 & 1 \\
0 & 1 & 0 & 0 & 1 & 0 & 1 & 1 \\
0 & 0 & 1 & 1 & 0 & 1 & 0 & 1 \\
0 & 0 & 0 & 0 & 0 & 1 & 0 & 1
\end{pmatrix}
\]

(2)

The function δ⁻¹ does the reverse conversion. We have not used any transformation function (δ or δ⁻¹) in the S-box operation (Figure 3). The elements of standard affine matrix used in S-box is defined over the composite field \(GF(2^8)\) [2]. The ByteSub (S-box) transformation is carried out in our design over the composite field \(GF((2^4)²)\). It is possible without imposing additional hardware overheads using the following technique:

- As discussed at Section 2, \(Y = AX^{-1} + B\). In the composite field,

\[
\delta(Y) = \delta(AX^{-1}) + \delta(B) = \delta(A\delta^{-1}(\delta(X^{-1}))) + \delta(B) = A'X' + \delta(B),
\]

where \(A' = \delta A \delta^{-1}\) and \(X' = (\delta(X))^{-1}\). \(A'\) becomes:

\[
A' = \begin{pmatrix}
0 & 0 & 1 & 0 & 1 & 0 & 0 & 0 \\
0 & 1 & 0 & 1 & 0 & 0 & 0 & 1 \\
0 & 0 & 1 & 0 & 0 & 1 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
1 & 0 & 1 & 0 & 0 & 1 & 0 & 0 \\
0 & 1 & 0 & 0 & 1 & 0 & 1 & 0 \\
0 & 0 & 1 & 0 & 1 & 0 & 1 & 0 \\
0 & 0 & 0 & 1 & 0 & 0 & 0 & 0
\end{pmatrix}
\]

(3)

- Every \(X \in GF((2^4)^2)\) can be represented as \((ax + b)\). The multiplicative inverse for an arbitrary polynomial \((ax + b)\) is given by: \((ax + b)^{-1} = a(a^2\lambda + ab + b^2)^{-1}x + (a + b)(a^2\lambda + ab + b^2)^{-1}\), where \(\lambda\) is a primitive element of \(GF(2^4)\).

Figure 3. Structure of Different S-boxes

Figure 4 depicts the corresponding block-diagram of three stage inverse multiplier. The primary goal of such design is to reduce hardware. The field polynomial used for the computations in \(GF(2^4)\) is \((x^4 + x + 1)\). The multiplication employs modulo arithmetic of an irreducible polynomial \((x^2 + x + \lambda)\), where \(\lambda\) is a primitive in \(GF(2^4)\).

There are four such polynomials, for each of which there are seven different transformation matrices (T) [5]. We choose \(\lambda = \omega^{14}\) for the best case result, where \(\omega = (0010)_2\) is an element in \(GF(2^4)\). The result is obtained out of logic synthesis with 0.18\(\mu\) technology with minimum gate-count of 273 gates and maximum latency of 2.93 ns.

In our design, the S-box table requires 32 instances in the encryption unit and 8 instances in the key scheduling part. This makes area optimization of a single S-box instance an important factor in terms of the overall hardware overhead. The factors controlling the size of an S-box are a combination of the design and the logic-synthesis effort. The elements of transformation matrix \(T\) are changed depending upon the values of \(\lambda\). So, choosing the appropriate value of \(\lambda\) is another factor to optimize the size of the S-box. The total number of '1' entries in the fixed affine matrix \(A\) [2] is equal to 40. The total number of '1' entries in our new defined affine matrix \(A'\) is equal to 18. Implementing the matrices in a straightforward way, the number of XORs would be equal to the number of '1' entries minus the number of rows in the matrices. This would lead to an XOR gate count of 10, which results in a reduction of 22 XOR gates. Figure 5 illustrates the area-latency curves of different existing S-box implementations, along with our
suggested one. The different area-latency values for a particular design are represented by the symbol (•). Three dots in the curve corresponding to our design has \( \lambda = (\omega^{14}, \omega^{12}, \omega^{11}) \). Our implementation is 1.047 times (286/273) better than the smallest one (Satoh at el. [6]) in terms of area.

Figure 5. Area-Latency tradeoff for S-box

4.2 Subfield Implementation of MixColumn

In Mixcolumn transformation, the elements of the fixed matrix \( M \) belongs to \( GF(2^8) \). Since, according to our design, all operations are in \( GF((2^4)^2) \), all elements of \( M \in GF(2^8) \) must be mapped into the elements of \( M' \in GF((2^4)^2) \). This is done using a transform matrix \( T \) (equation 2). For example, \( T(2) = 00101110 \) = \((\omega^{14} + x \omega)\), where \( \omega \) is the primitive element of \( GF(2^4) \) and the irreducible polynomial for \( GF((2^4)^2) \) is \((x^2 + x + \omega^{14})\). Figure 6 shows the structure of the MixColumn transformation.

Figure 6. Structure of the MixColumn

5 Key Schedule Optimization

All computations on key expansion occur wordwise (32-bit). Let \( N_k \) denotes the length of the key divided by 32 and \( N_b \) denotes the length of the data block divided by 32. Let \( W[0] \), \ldots, \( W[N_k - 1] \) be the \( N_k \) columns of the original key. These \( N_k \) columns can be recursively expanded to obtain \( N_k \times N_r \) more columns (RoundKey), where \( N_r \) is the number of round. The values of \( N_r \) are determined from the Table 2 [2]. Suppose that all columns up to \( W[i - 1] \) have been expanded. The next column \( W[i] \) can be constructed as:

\[
W[i] = \begin{cases} 
W[i-N_b] \oplus T(W[i-1]) & \text{if } i \text{ mod } N_k = 4(N_k = 8) \\
W[i-N_b] \oplus T(W[i-1],Rcon) & \text{if } i \text{ mod } N_k = 0 \\
W[i-N_b] \oplus W[i-1] & \text{otherwise}
\end{cases}
\]

Table 2. Numbers of rounds \( (N_r) \) as a function of the block and key length

<table>
<thead>
<tr>
<th>( N_k )</th>
<th>( N_b=4 )</th>
<th>( N_b=6 )</th>
<th>( N_b=8 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( N_k=4 )</td>
<td>10</td>
<td>12</td>
<td>14</td>
</tr>
<tr>
<td>( N_k=6 )</td>
<td>12</td>
<td>12</td>
<td>14</td>
</tr>
<tr>
<td>( N_k=8 )</td>
<td>14</td>
<td>14</td>
<td>14</td>
</tr>
</tbody>
</table>

Figure 7. KeyScheduler

Here \( T(W[i-1],Rcon) \) is a non-linear transformation based on the application of the S-box to the four bytes of the column, and the addition of a round constant (Rcon) for symmetry elimination [2]. \( T(W[i-1]) \) represents the same without addition of Rcon. In Figure 7, the \( W \)'s are the 32-bit shift registers. Initial key is generated from control unit, \( C_1 \) is user-specific and \( i \) is generated from an 8-bit up counter which is reset set to value 1 by the Data_enable signal. The Data_enable signal is set when data blocks are ready to be processed. \( R \) is a 256-bit register to store initial key. When Data_enable signal is set, a single word (32 bits) among \( N_k \) words goes through the shift registers \( W[N_k-8], \ldots, W[N_k-1] \) at every clock. The word is selected by 3 bits control signals generated by the counter. \( W[N_k-8], \ldots, W[N_k-1] \) are occupied by the initial key stored at register \( R \). Now at every clock single word of RoundKey is made. It goes through another set of 32-bit shift registers \( W[N_k-7], \ldots, W[N_k+7] \) as round key and the same key is fed back to the register \( W[N_k-1] \) through the multiplexer \( M1 \) for generating the next round key. The architecture takes \( N_b \) clock cycles to generate single round key. A maximum of \( 8 \times 14 = 120 \) clock cycles are required to generate complete round key (for 256 bits data and key). The primary goal of this architecture is to have a drastic reduction in hardware as compared to [5, 6, 10, 16].

6 The Control Unit

A Finite State Machine with Data-path (FSMD) is a universal specification model [12] which is used in the core of the present work with the addition of a reset state. This reset state can be treated as the start state of the FSMD.
Figure 8. FSM of Control Unit

In the Figure 8, \{S_0, S_1, S_2, S_3, \ldots, S_{36}\} are the set of control states. \(S_0\) = reset state, \{clock, reset, \(C_2C_1\)\} = input signals. \(O_0, O_1, O_2, O_3, O_4, O_5\) are the output signals where \(O_0 = \text{Key enable}, O_1 = \text{Data enable}, O_2 = \text{Initial key}, O_3 = \text{Addkey enable}, O_4 = \text{First round} \) and \(O_5 = \text{Last round}. \(C_2C_1\) is a 4-bit control signal specified by user. The lower 2-bit \(C_1\) specifies the key length and higher 2-bit \(C_2\) specifies the block length.

The Key_enable signal loads the initial key into the register \(R\) shown in Figure 7. Data_enable signal select 256 bits block among two 256 bits blocks, one coming from Plain Text and other generated as intermediate cipher shown in Figure 2. This signal is also used to initiate the value of the Counter shown in Figure 7. Figure 2 takes two clock cycles to complete a single round, but KeyScheduler (Figure 7) takes a minimum of 4 cycles for generating single round key. This is why Addkey enable signal is used as an enable signal of BUFFER2 to get valid data from xor operation (Figure 2). Similarly, Last_round signal is used as an enable signal of BUFFER3 to get valid Cipher Text.

According to our design, the state transitions of the controller take place at every clock cycle. If the controller waits for \(j \geq i\) clock cycles at state \(S_i\) then the next state is \(S_j\) and the controller self loops at \(S_j\) for \((j-i)\) clock cycles. The transitions make several branches depending upon the control signal \(C_2C_1\). Values of \(C_2C_1\) for different values of key and data length are shown in Figure 3. We need total \((N_b + N_r + N_k)\) states, i.e, \(8x1448 = 120\) states for 256 bits block and key length. But due to short of scope only 86 states are shown in the figure, through which it can be explained how does the FSM work. Let us take an example.

**Example 1** In the example let us take 128 bits data and 128 bits key (i.e \(C_2C_1 = 0000\)).

- The controller starts at \(S_0\) with the positive edge of reset. The consecutive 15 clock cycles states \\{\(S_0, S_1, \ldots, S_{15}\)\} have same status and in those cases all outputs are 0.
- At the next state \(S_{16}\) (16th cycle) Key_enable signal becomes 1 and rest are 0. It signifies that 128 bits data are stored in register \(R\) as initial key. As we are taking 8 bits data from I/O at every cycle, after 16 cycles we can get 128 bits data.

- In next cycle (state \(S_{17}\)) all output signals are set to 0. Similarly after 15 cycles at state \(S_{32}\) Data_enable and Initial_key are set to 1. In consecutive 4 cycles Initial_key signal sets to 1. At these stages Max M1 selects 4 words from \(R\) (Figure 7) and those words are stored in shift registers \(W[N_k - 4], \ldots, W[N_k - 1]\), i.e, \(W[0], \ldots, W[3]\). Now the words of the key are ready to be expanded.

- At next 4 cycles 128 bits round key is made. At \(S_{38}\) there are three branching \(S_{39}, S_{40}\) and \(S_{41}\). Those branching take place depending upon the signals Last_round and First_round.

- All those states except \(S_{40}\) come back to \(S_{36}\) in the next cycle signifying that the expansion of next round keys can start. State \(S_{40}\) comes back to \(S_{32}\). It signifies that all 10 rounds key generation are completed and ready to store initial keys from register \(R\) to the shift registers \(W[N_k - 4], \ldots, W[N_k - 1]\), i.e, \(W[0], \ldots, W[3]\) to generate next 10 round key for next cipher text.

\[
\begin{array}{c|c|c|c}
\hline
C_2C_1 & Key & 128 & 192 & 256 \\
\hline
Data & 128 & 0000 & 0100 & 1000 \\
 & 192 & 0001 & 0101 & 1001 \\
 & 256 & 0010 & 0110 & 1010 \\
\hline
\end{array}
\]

**Table 3.** \(C_2C_1\) for different Key and Data

7 Implementation Results and Comparison

The proposed design has been implemented on Xilinx Vertex XCV1000 hardware platform and simulated by ModelSim8.1i. The same design has been compiled in 0.18 \(\mu\) CMOS using Synopsys design tool (Design Compiler). The performances (throughput and frequency) are shown at Table 4 and Table 5. Throughput \((\tau)\) is calculated as:

\[
\tau = (\eta \times f) / \psi, \quad \text{where} \quad \eta, f \text{ and } \psi \text{ stand for block length, clock frequency and number of clock cycle respectively.}
\]

In our design \(N_b\) clock cycles are needed to generate single round intermediate cipher.

\[
\tau = (N_b \times 32 \times f) / (N_b \times N_r) = (32 \times f) / N_r.
\]
8 Conclusions

We have presented AES encryptor core design in rolling and inner-pipelined fashion. The design strikes an optimal balance between area and frequency of operation. Results and comparisons with existing works have been furnished. The paper demonstrates that the proposed architecture outperforms prior results with respect to the parameter throughput per area. Implementation of encryptor/decryptor core designs into a single-chip exploiting extended composite subfield $GF(((2^2)^2)^2)$ may be included as a future work.

References